

Deep Reinforcement Learning based Optimal Energy System Scheduling

Hou Shengren



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Self-Introduction



Shengren (侯胜任) Hou (He/Him)

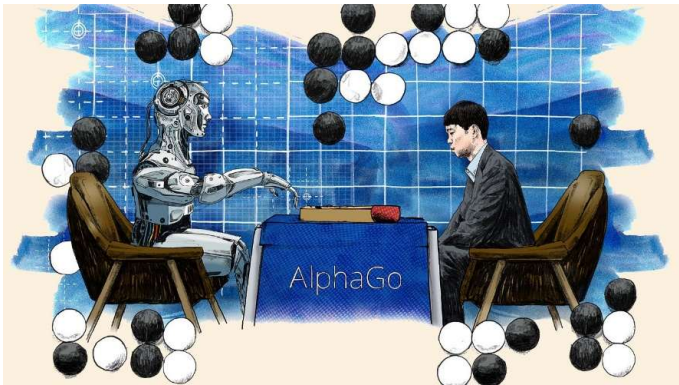
Quantitative Power Trader @ OTC FLOW | PhD in Power System and AI | Co-founder of Energy Quant Research Institution

Delft, South Holland, Netherlands · [Contact info](#)

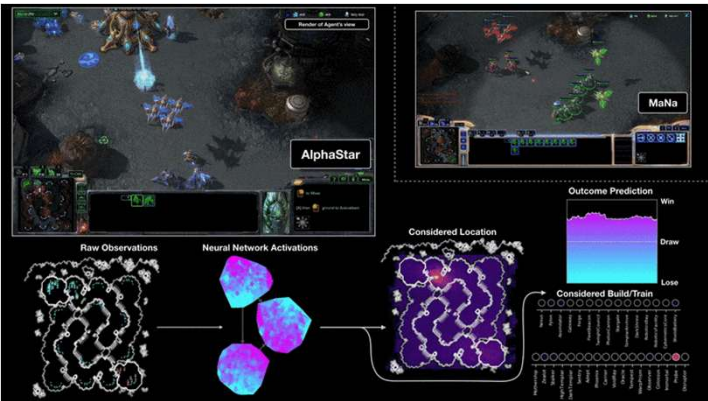
1. Researcher (Power and financial market, Power System, AI)
2. Career (Quantitative Power Trader, Power market expert)
3. Entrepreneur (Energy Quant Research Institution)
4. Social activity (Board member of VCWI)



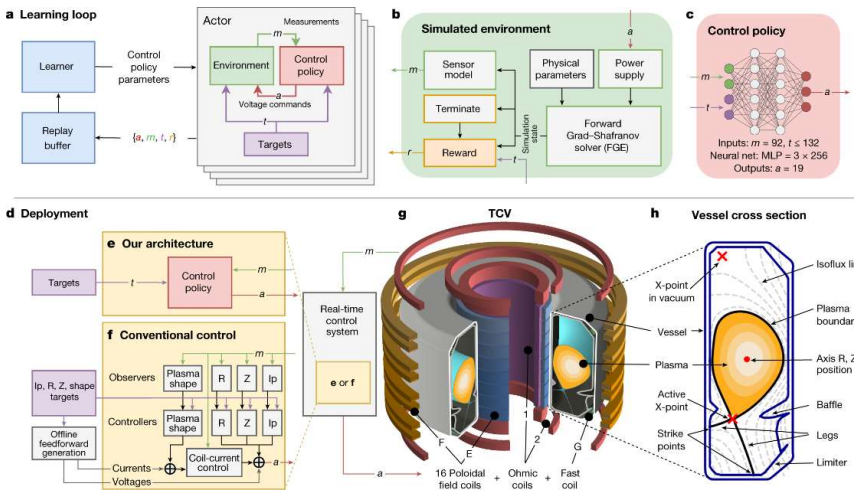
Reinforcement Learning Introduction



2014

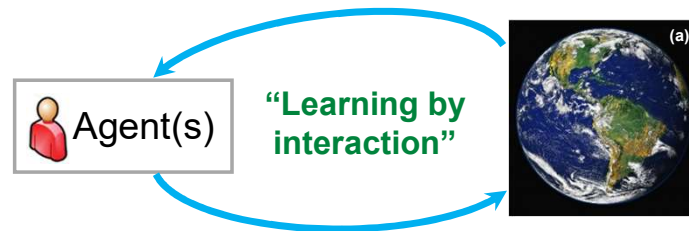


2018



2022

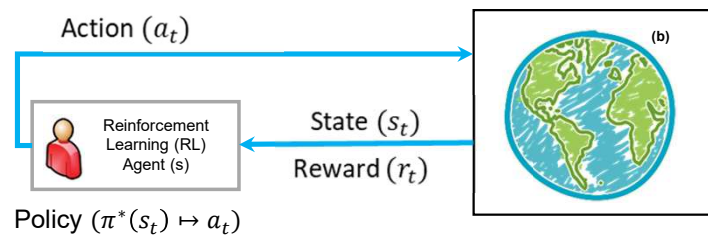
Active distribution networks (ADNs) operation as a RL problem



RL solves a sequential problem that is formulated as a Markov Decision Problem (MDP):

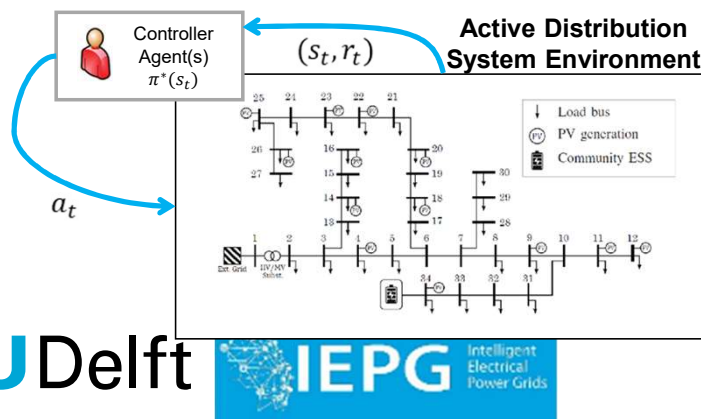
$$\langle S, A, P, r, \gamma \rangle$$

S : State space (Observed variables)
 A : Action space (possible control actions)
 P : Transition probability (Not available but simulated)
 r : Reward function (Signal to maximize)
 γ : Discount factor (importance of future rewards)

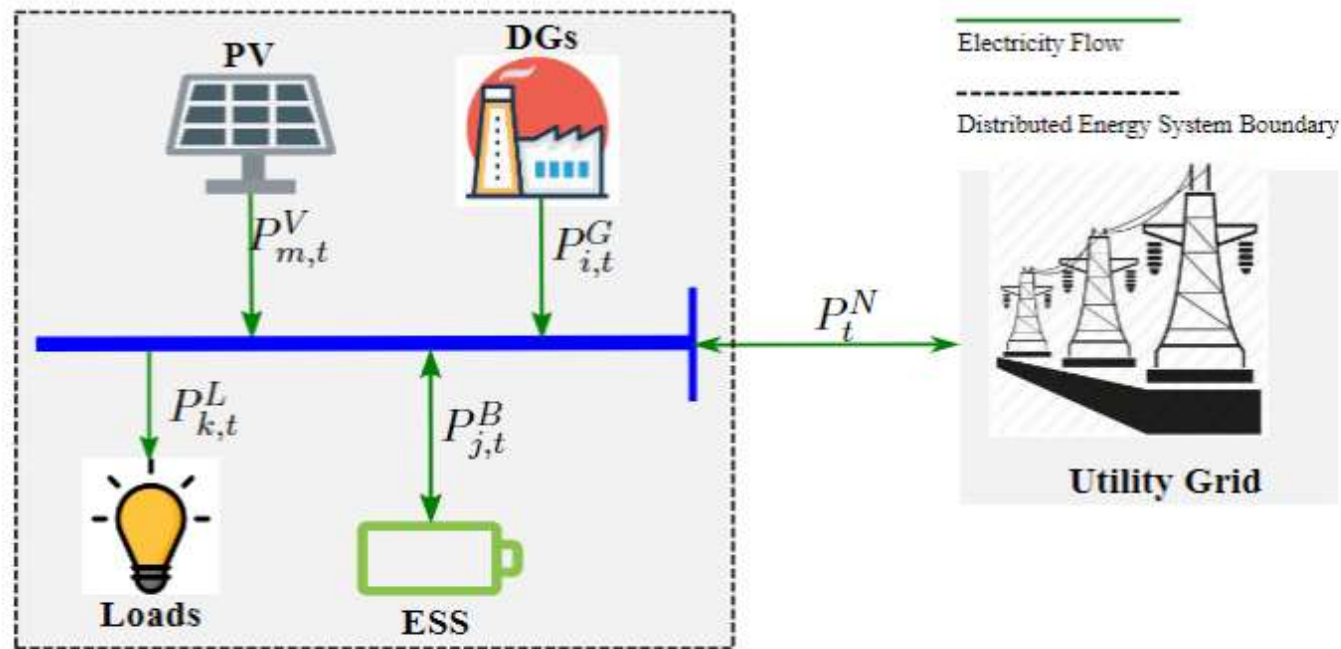


Advantages of RL:

- It is a "model-free" approach to solve decision-making problems.
- Excellent generalization features. Optimal actions for different states.
- Complexity of the system (environment) can be high. Using powerful parametrized function approximators for $\pi(s, \theta)$ (e.g. Deep Neural Networks), we can find good and practical solutions.



Experiment Design



Research Background: What is optimal energy system scheduling?

$$\min \sum_{t \in \mathcal{T}} \sum_{i \in \mathcal{G}} (C_{i,t}^G + C_t^E) \Delta t \quad (1)$$

$$C_{i,t}^G = a_i \cdot (P_{i,t}^G)^2 + b_i \cdot P_{i,t}^G + c_i, \quad i \in \mathcal{G}. \quad (2)$$

$$C_t^E = \begin{cases} \rho_t P_t^N & P_t^N > 0, \\ \beta \rho_t P_t^N & P_t^N < 0. \end{cases} \quad (3)$$

Minimize energy costs

Subject to:

$$\sum_{i \in \mathcal{G}} P_{i,t}^G + \sum_{m \in \mathcal{V}} P_{m,t}^V + P_t^N + \sum_{j \in \mathcal{B}} P_{j,t}^B = \sum_{k \in \mathcal{L}} P_{k,t}^L, \forall t \in \mathcal{T} \quad \Rightarrow \text{Power balance constrain}$$

$$\underline{P}_i^G \cdot u_{i,t} \leq P_{i,t}^G \leq \bar{P}_i^G \cdot u_{i,t} \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (4)$$

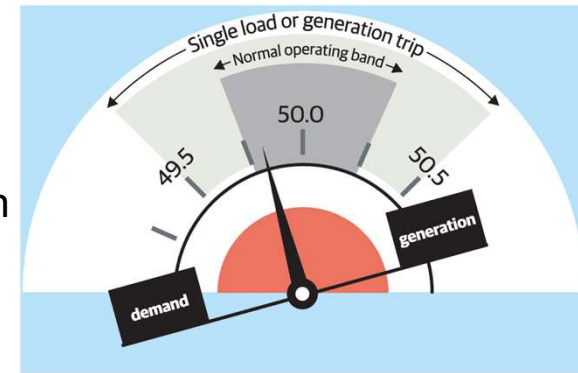
$$\underline{P}_{i,t}^G - P_{i,t-1}^G \leq RU_i \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (5)$$

$$P_{i,t}^G - P_{i,t+1}^G \leq RD_i, \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (6)$$

$$-\underline{P}_j^B \leq P_{j,t}^B \leq \bar{P}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (7)$$

$$-P_j^B \leq P_{j,t}^B \leq \bar{P}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (8)$$

Technical limits for generators



Mathematical essence is to search for optimal solution for **sequential decision problems** within limited time window.

Case Study: Energy System Optimal Scheduling

$$\min_{P_{i,t}^G, P_{j,t}^B} \left\{ \sum_{t \in \mathcal{T}} \sum_{i \in \mathcal{G}} [C_{i,t}^G(\cdot) + C_{i,t}^E(\cdot)] \Delta t \right\}, \quad (1)$$

$$C_{i,t}^G = a_i (P_{i,t}^G)^2 + b_i P_{i,t}^G + c_i, \quad \forall i \in \mathcal{G}. \quad (2)$$

$$C_t^E = \begin{cases} \rho_t P_t^N & P_t^N > 0, \\ \beta \rho_t P_t^N & P_t^N < 0. \end{cases} \quad (3)$$

Minimization of all operational cost

Subject to:

$$\sum_{i \in \mathcal{G}} P_{i,t}^G + \sum_{m \in \mathcal{V}} P_{m,t}^V + P_t^N + \sum_{j \in \mathcal{B}} P_{j,t}^B = \sum_{k \in \mathcal{L}} P_{k,t}^L, \quad \forall t \in \mathcal{T} \quad (4)$$

Power balance constraint

$$\underline{P}_i^G \leq P_{i,t}^G \leq \overline{P}_i^G \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (5)$$

$$P_{i,t}^G - P_{i,t-1}^G \leq RU_i \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (6)$$

$$P_{i,t}^G - P_{i,t+1}^G \leq RD_i \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (7)$$

$$-P_j^B \leq P_{j,t}^B \leq \overline{P}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (8)$$

$$SOC_{j,t}^B = SOC_{j,t-1}^B + \eta_B P_{j,t}^B \Delta t / E_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (9)$$

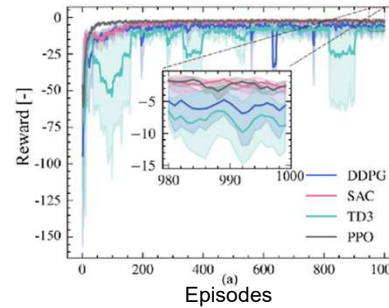
$$SOC_j^B \leq SOC_{j,t}^B \leq \overline{SOC}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (10)$$

$$-\overline{P}^C \leq P_t^N \leq \overline{P}^C \quad \forall t \in \mathcal{T} \quad (11)$$

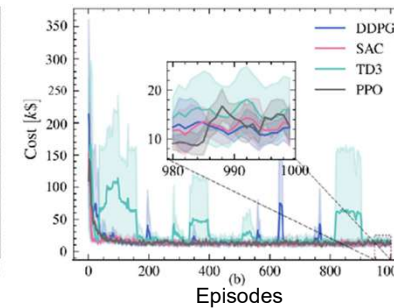
Operational constraints

$$r_t(s_t, a_t) = -\sigma_1 \left[\sum_{i \in \mathcal{G}} C_{i,t}^G + C_t^E \right] - \sigma_2 \Delta P_t$$

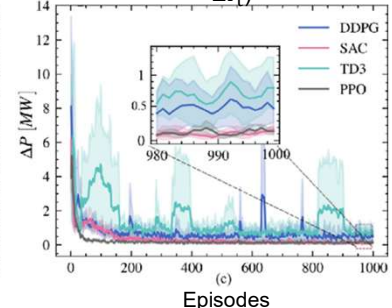
Overall training



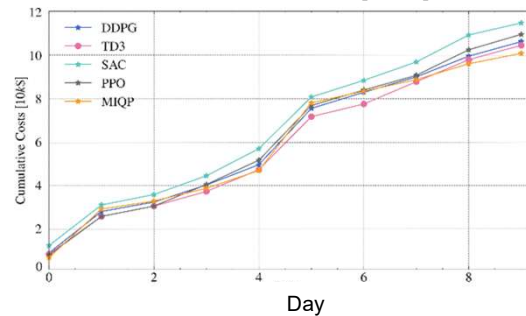
Training (Cost component)



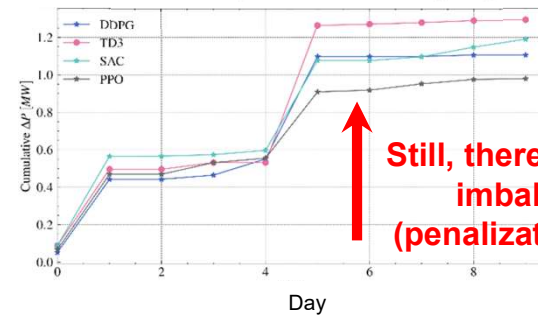
Training (Imbalance component ΔP_t)



Cumulative costs [€10k]



Cumulative power imbalance ΔP [MW]



(D)RL algorithms *lack of safety guarantees*, as they cannot (yet) be directly imposed in the algorithm's formulation.

Our idea and experiments validation

Goal

Reinforcement learning algorithms that can provide theoretical proof of the constraint handling, during the energy management operation.

Background

- providing such proof of RL algorithms can be difficult and may not always be feasible.
- This is because the lack of mathematical tools and theories for RL algorithms

Motivation

- Classic model based approaches like MPC, MILP have well-established mathematics theories. We can formulate the trained RL algorithm as a MIP, which can bring a stronger theoretical foundation for RL algorithms.
- In this way, Various mathematical theories can be used for ensuring the feasibility of our algorithm, such as duality theory, convex optimization, or polyhedral theory.



Case Study: Energy System Optimal Scheduling

Understanding the (operational) constraints in the action space:

Subject to:

$$\sum_{i \in \mathcal{G}} P_{i,t}^G + \sum_{m \in \mathcal{V}} P_{m,t}^V + P_t^N + \sum_{j \in \mathcal{B}} P_{j,t}^B = \sum_{k \in \mathcal{L}} P_{k,t}^L, \forall t \in \mathcal{T} \quad (4)$$

$$\underline{P}_i^G \leq P_{i,t}^G \leq \overline{P}_i^G \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (5)$$

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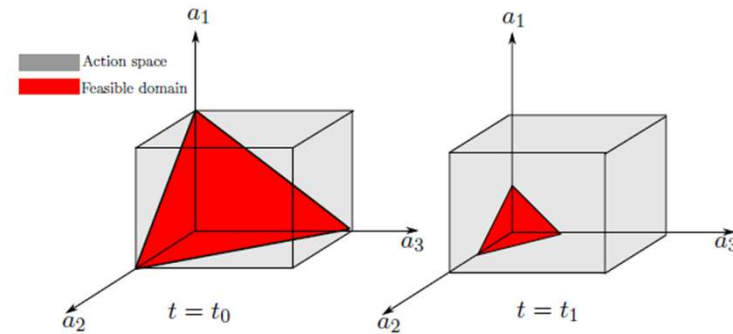
$$P_{i,t}^G - P_{i,t+1}^G \leq RD_i \quad \forall i \in \mathcal{G}, \forall t \in \mathcal{T} \quad (7)$$

$$-\underline{P}_j^B \leq P_{j,t}^B \leq \overline{P}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (8)$$

$$SOC_{j,t}^B = SOC_{j,t-1}^B + \eta_B P_{j,t}^B \Delta t / E_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (9)$$

$$\underline{SOC}_j^B \leq SOC_{j,t}^B \leq \overline{SOC}_j^B \quad \forall j \in \mathcal{B}, \forall t \in \mathcal{T} \quad (10)$$

$$-\overline{P}^C \leq P_t^N \leq \overline{P}^C \quad \forall t \in \mathcal{T} \quad (11)$$



The equality constraint defines the **feasible action space** (red space, hyperplane) as a **subspace** of the action space (grey space).

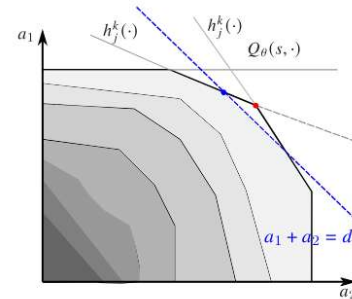


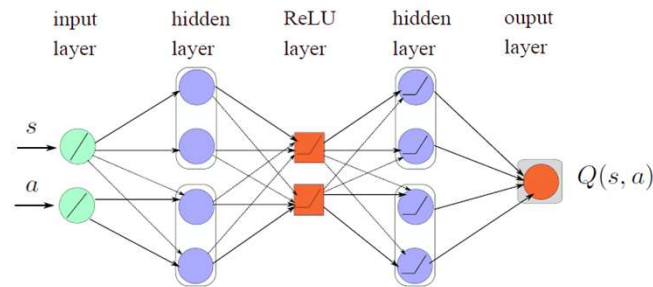
Figure 2.4: Visualization of the constraint space whose boundaries are formed by the hyperplanes $h_j^k(\cdot)$ defined by the ReLU activation functions derived from the deconstructed DNN $Q_\theta(s, \cdot)$ as a MIP formulation, for a specific state s and actions a_1 and a_2 . The grey area shows the increasing value (from darker to lighter) of $\forall Q_\theta$. The red point exemplifies the optimal solution of $\max_{a \in \mathcal{A}} Q_\theta(s, \cdot)$ if constraint $a_1 + a_2 = d$ is disregarded. If such a constraint is added to the MIP formulation, the solution represented with the blue point will be reached.

Case Study: Energy System Optimal Scheduling

To strictly enforce the power balance constraint:

Deep neural networks +
combinatorial optimization.

(MIP-DQN)



$$\max_{a \in \mathcal{A}, x_j^k, s_j^k, z_j^k, \forall k} \quad \{(21)\}$$

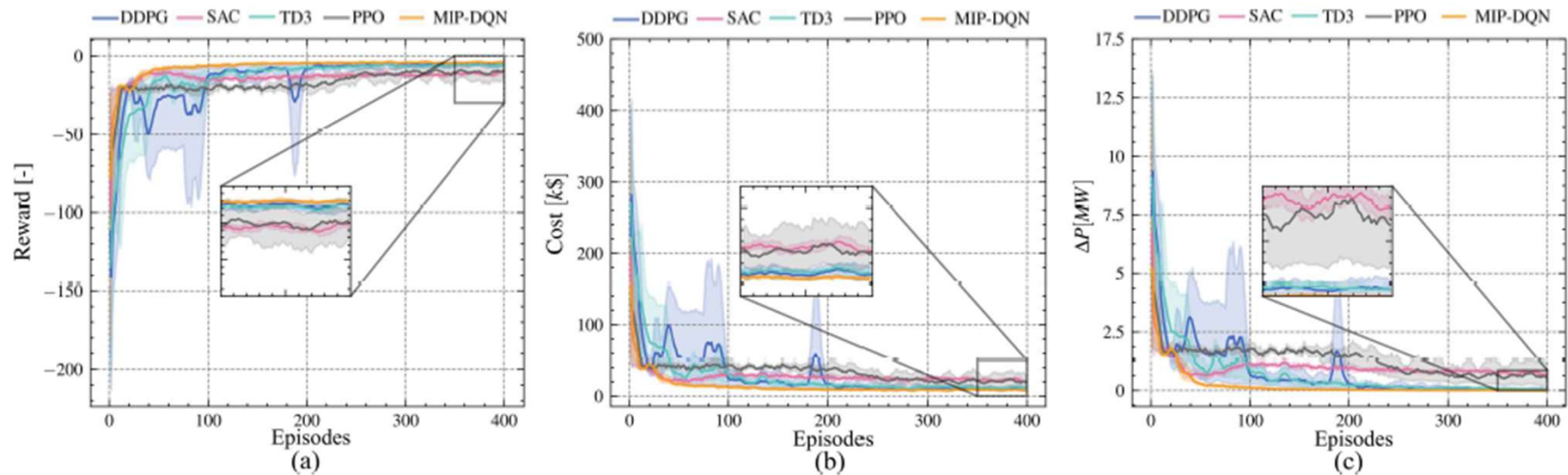
$$\left. \begin{aligned} \sum_{i=1}^{l_{k-1}} w_{ij}^{k-1} x_i^{k-1} + b_j^{k-1} &= x_j^k - s_j^k \\ x_j^k, s_j^k &\geq 0 \\ z_j^k &\in \{0, 1\} \\ z_j^k = 1 &\rightarrow x_j^k \leq 0 \\ z_j^k = 0 &\rightarrow s_j^k \leq 0 \end{aligned} \right\} \forall k, \forall j, \quad (22)$$

$$lb_j^0 \leq x_j^0 \leq ub_j^0, \quad j \in l_0, \quad (23)$$

$$\left. \begin{aligned} lb_j^k &\leq x_j^k \leq ub_j^k \\ \overline{lb}_j^k &\leq s_j^k \leq \overline{ub}_j^k \end{aligned} \right\} \forall k, \forall j. \quad (24)$$

$$\sum_{i \in \mathcal{G}} P_{i,t}^G + \sum_{m \in \mathcal{V}} P_{m,t}^V + P_t^N + \sum_{j \in \mathcal{B}} P_{j,t}^B = \sum_{k \in \mathcal{L}} P_{k,t}^L, \forall t \in \mathcal{T}$$

Case Study: Energy System Optimal Scheduling



During training, all tested algorithms seem to have similar convergence properties.

None of these algorithms are able to strictly enforce constraints, as expected. Nevertheless, the proposed MIP-DQN algorithm showed the lower error.

Case Study: Energy System Optimal Scheduling

Testing with unseen operational scenarios (uncertain PV and demand):

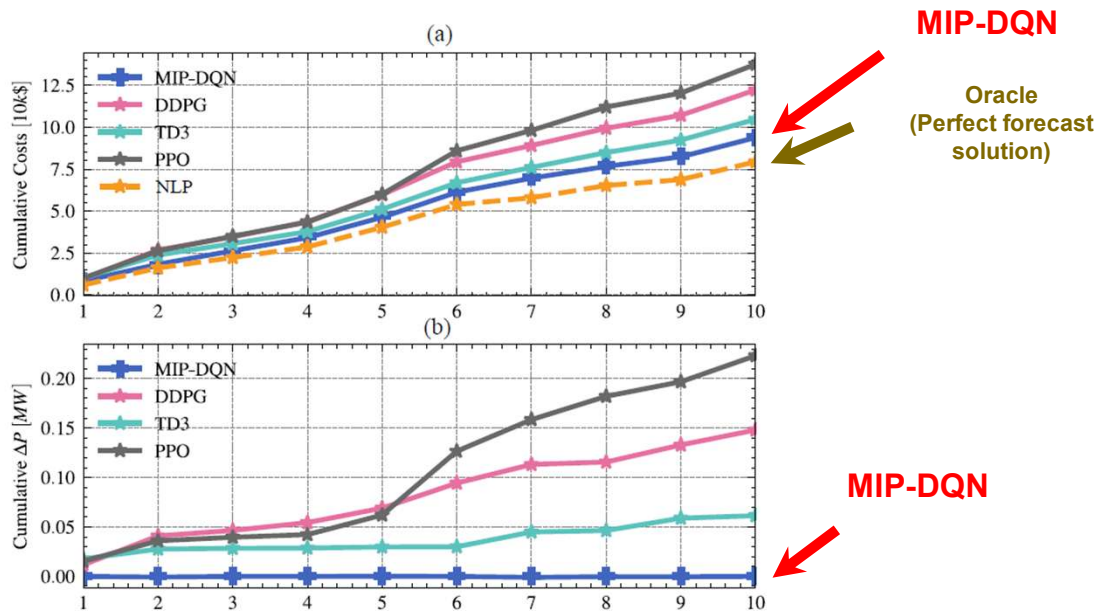


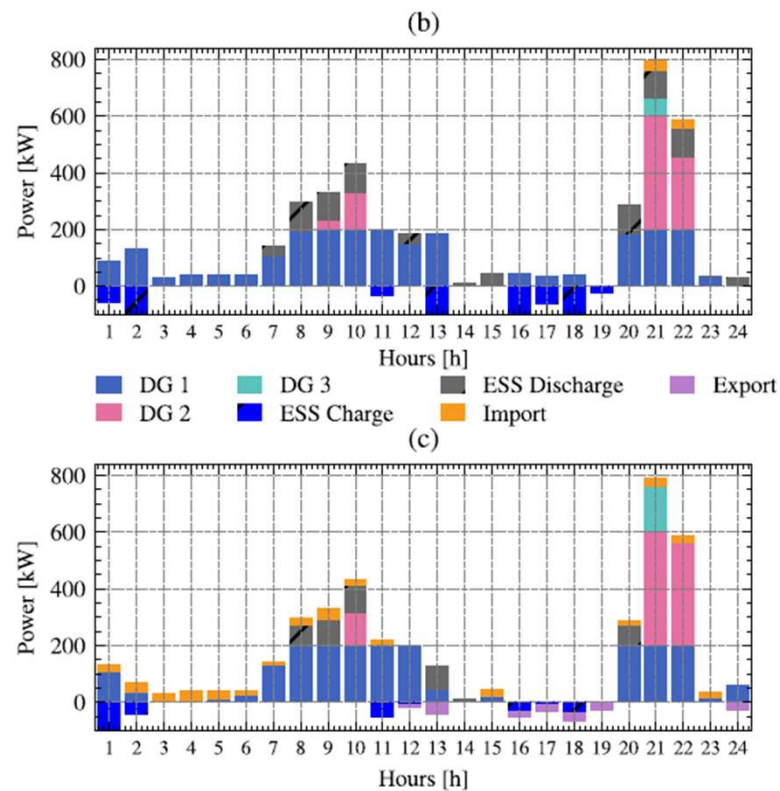
Table 4: Performance comparison of different DRL algorithms in a new test set of 30 days.

Algorithms	Error	ΔP [MW]	Computational time [s]
MIP-DQN	$13.7 \pm 0.3\%$	0.0	17
DDPG	$47.3 \pm 1.9\%$	0.14 ± 0.021	4.3
TD3	$31.5 \pm 0.7\%$	0.06 ± 0.011	4.9
PPO	$52.4 \pm 0.3\%$	0.15 ± 0.007	4.3

The MIP-DQN algorithm **strictly** meets the power balance constraint. Other SoA algorithms fail to do so.

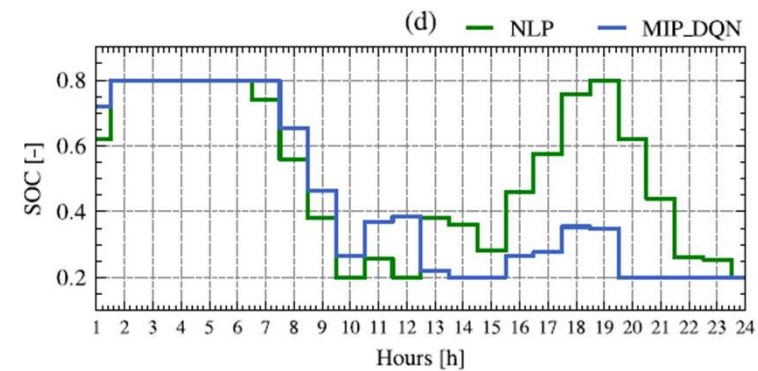
MIP-DQN algorithm achieves **lower** (average) errors when compared with other DRL algorithms.

Case Study: Energy System Optimal Scheduling



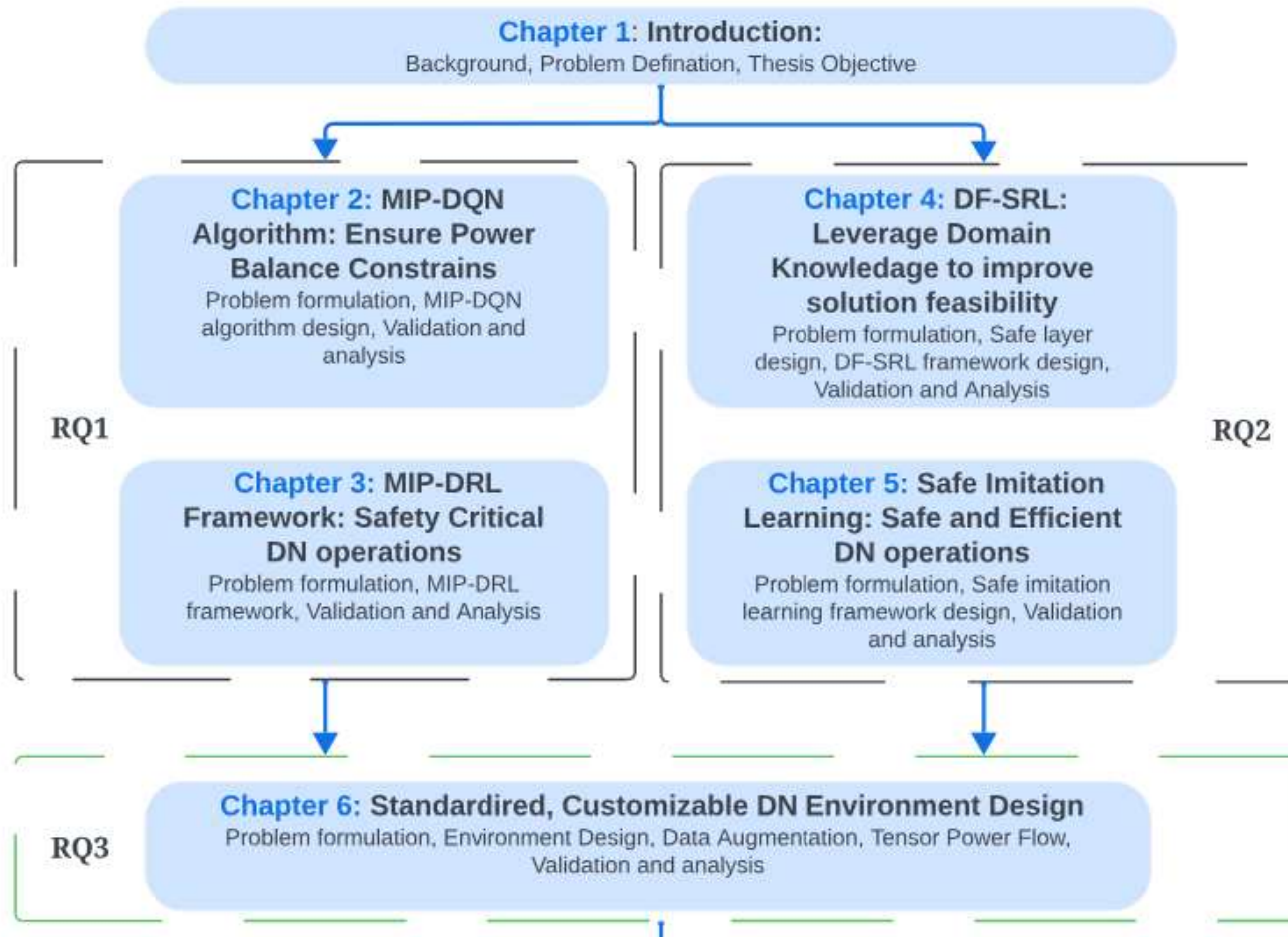
The MIP-DQN algorithm was able to define *similar* hourly operational schedule when compared with the optimal global solution.

Main difference: The MIP-DQN algorithm makes decision based only on current information, while the optimal global requires estimation of future values for the stochastic variables.



Future improvement: Look better into the future. Reduce error and learn from less data (data efficiency)

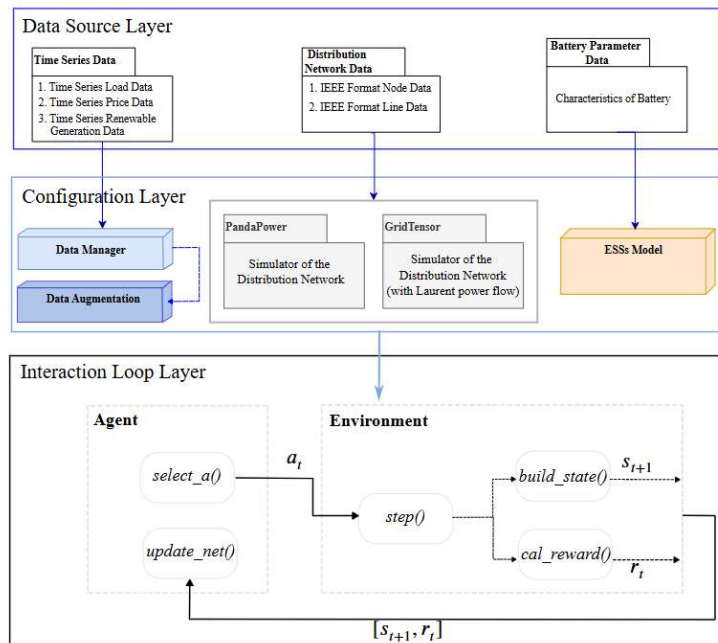
My PhD Routine



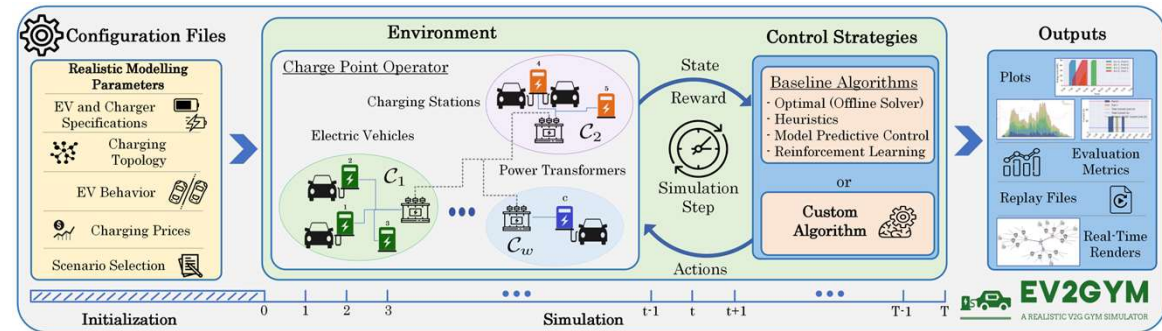
1. Stay Curious
2. Design or find out your own reward function

Some Open-source package we developed

RL-AND: An environment for ESSs dispatch in distribution network



EV2Gym: A Realistic EV-V2G-Gym Simulator for EV Smart Charging



<https://github.com/ShengrenHou>

<https://github.com/distributionnetworksTUDelft>



Distribution Networks TU Delft
distributionnetworksTUDelft



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